

$$C_{eff} = 2C$$

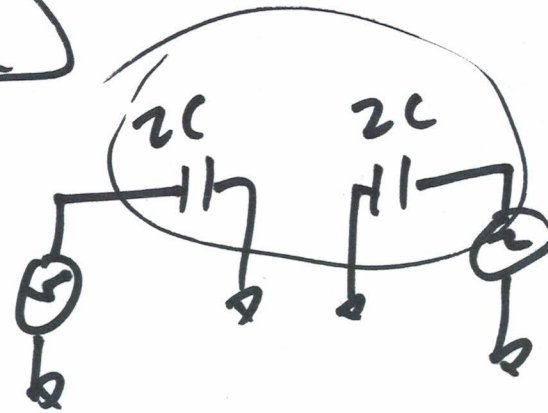
$$\frac{Q}{CV}$$

$$Q = CV$$

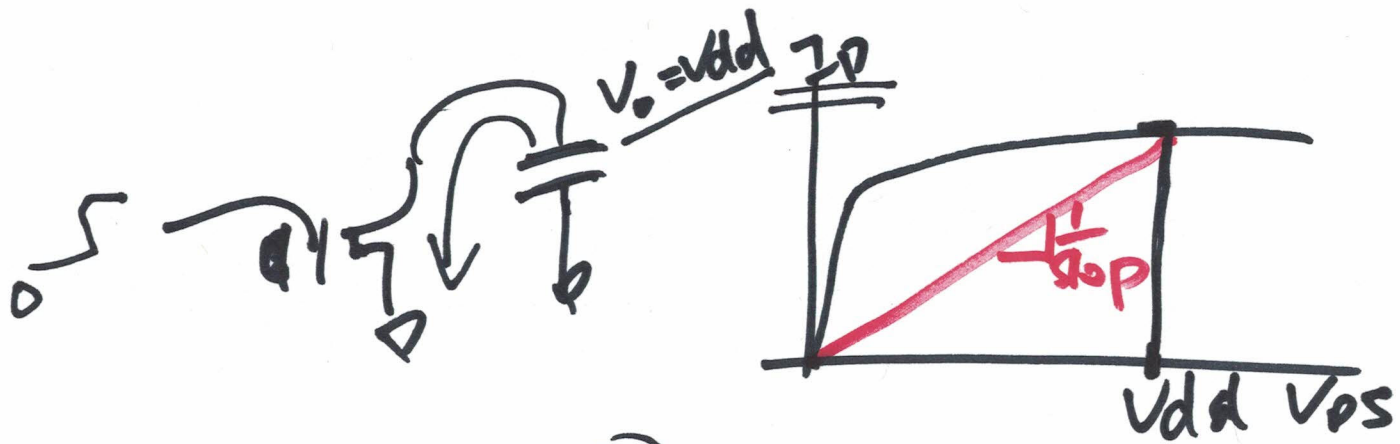
$$\Delta Q = v_{dd} \cdot C_{eff} = 2Q$$

~~$$C \cdot v_{dd} = Q$$~~

$$C_{eff} = 2C$$

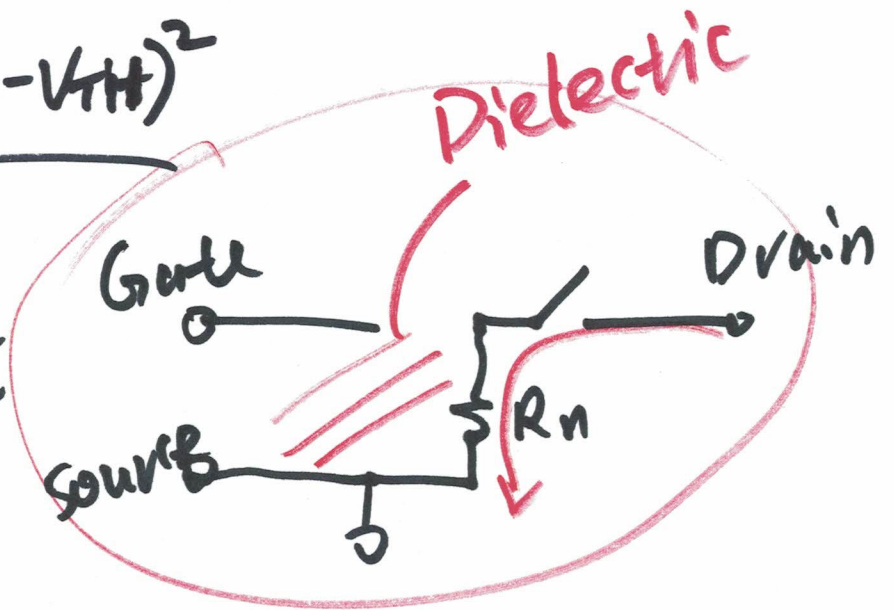


Miller Effect

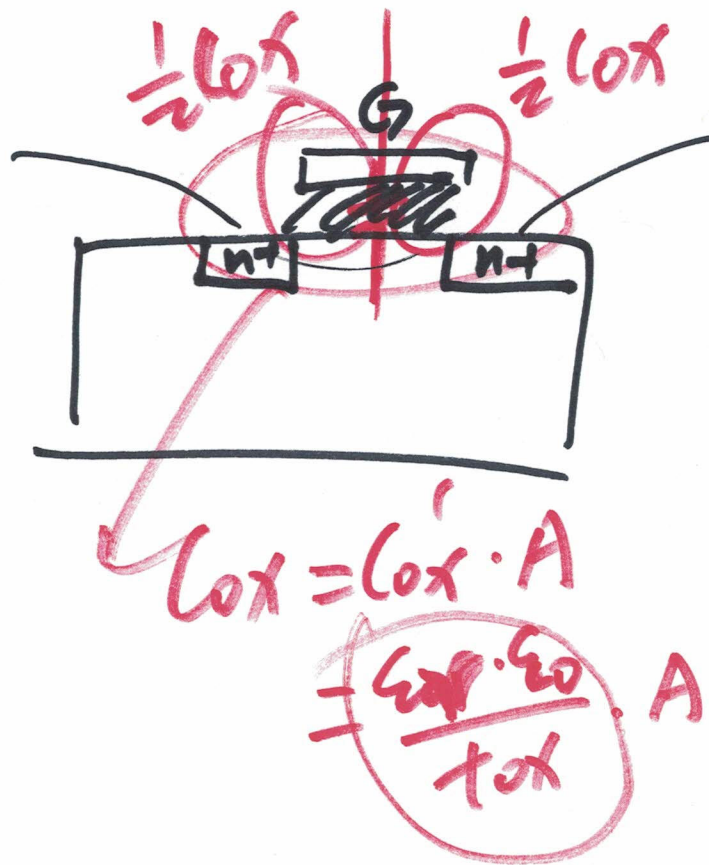
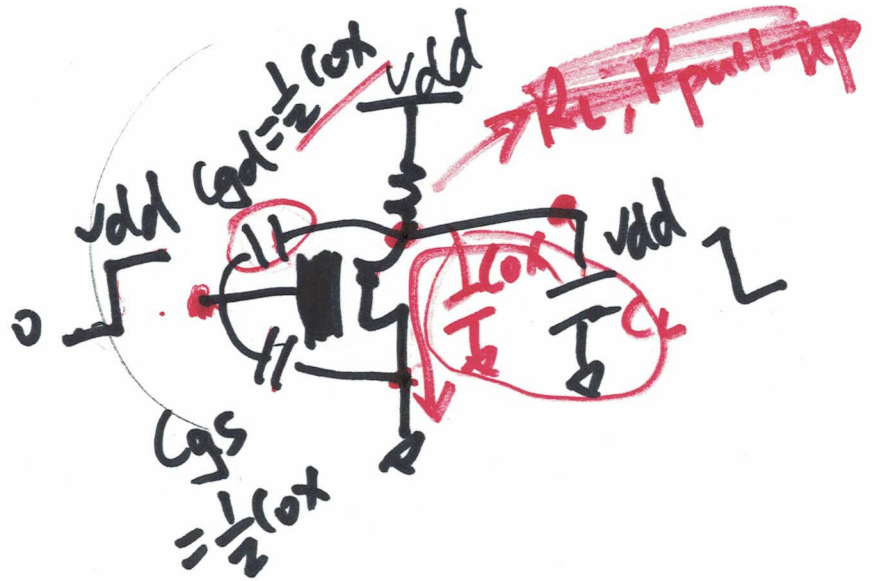


$$\text{slope} = \frac{t_p}{V_{dd}} = \frac{\frac{K_p n}{2} \frac{W}{L} (V_{GS} - V_{TH})^2}{V_{dd}}$$

$$R_n = \frac{1}{\text{slope}} = \frac{V_{dd}}{\frac{K_p n}{2} \frac{W}{L} (V_{GS} - V_{TH})^2}$$



2

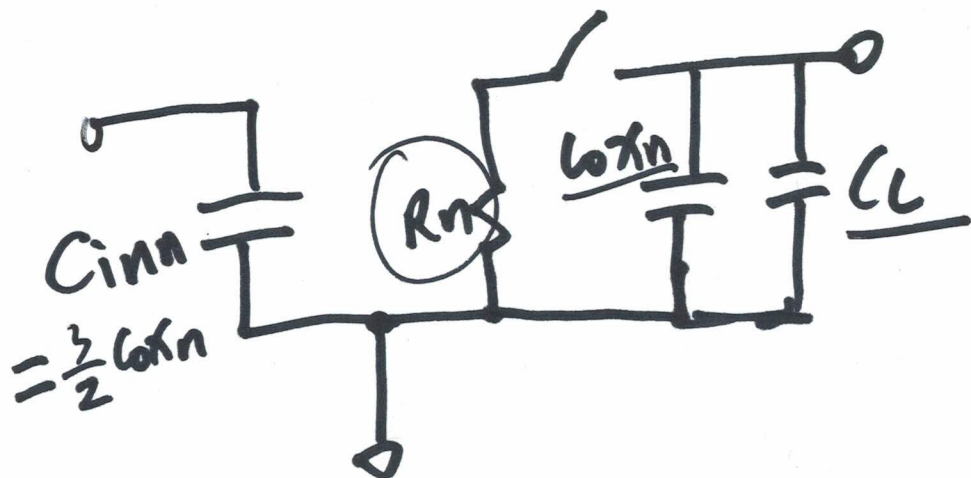


$$C_{ox} = C_{ox}' \cdot A$$

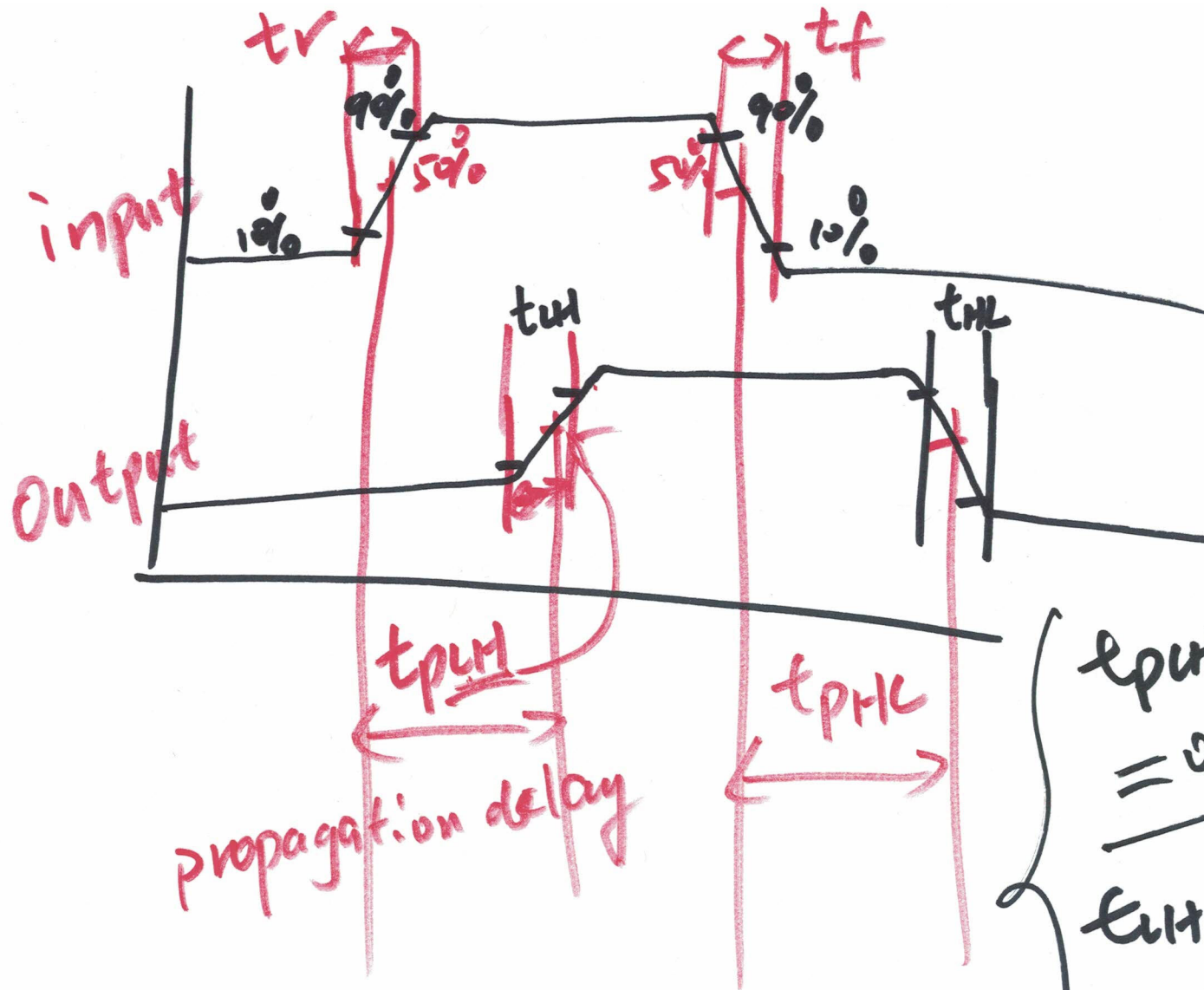
$$= \frac{\epsilon_{ox} \cdot \epsilon_0}{t_{ox}} \cdot A$$

$$C_{eff} = C_{gs} + 2C_{gd}$$

$$= \frac{3}{2} C_{ox}$$



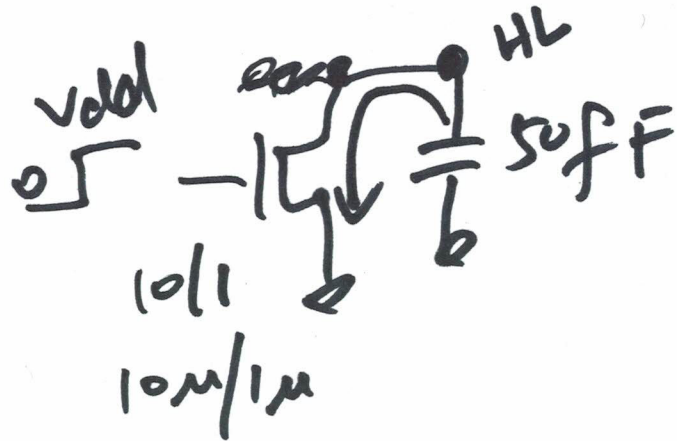
2



$$t_{pHL}, t_{pLH} = 0.7RC$$

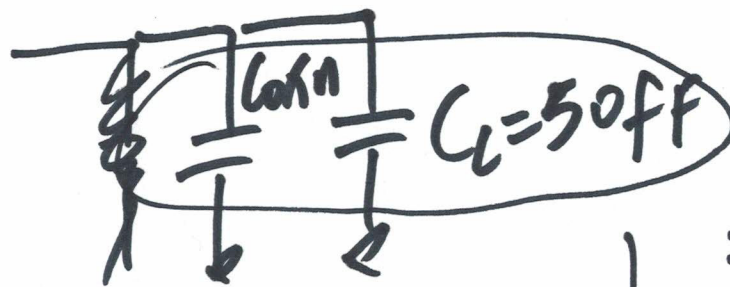
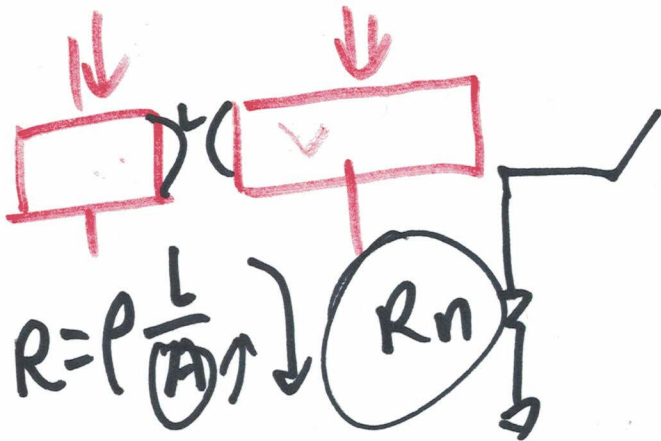
$$t_{uH}, t_{fL} = \frac{2.2RC}{(PSO \text{ of the CMOS Book})}$$

Example: t_{LH} t_{HL} t_{PHL} , t_{PLH}
 estimate the rise, fall, and delay times (output signal) of the following circuit. (P320)



	size	$R_{n,p}$	$C_{oxn,p}$
NMOS	10 μm/1 μm	1.5K	17.5 fF
PMOS	30 μm/1 μm	1.5K	52.5 fF

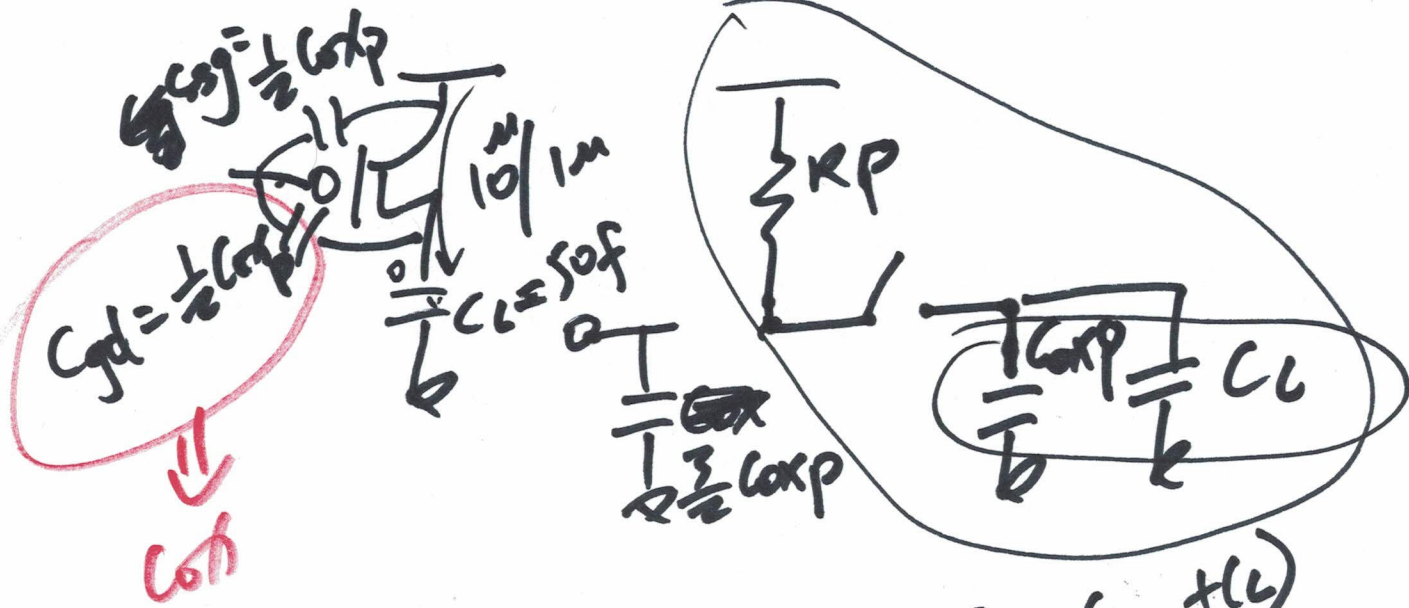
1 μm P317



$$\begin{aligned}
 t_{LH} &= t_{HL} = 2.2 RC \\
 &= 2.2 \times R_n \cdot (C_{oxn} + C_L) \\
 &= 2.2 \times 1.5K \cdot (17.5 + 50) \\
 &= 220 \text{ ps}
 \end{aligned}$$

$$\begin{aligned}
 t_{PHL} &= 0.7 RC = 0.7 \cdot R_n \cdot (C_{oxn} + C_L) \\
 &= 0.7 \times 1.5K \cdot (17.5 + 50) = 70 \text{ ps}
 \end{aligned}$$

(5)



$$t_{2H} = 2.2 RC = \frac{2.2}{2.2} R_p (C_{exp} + C_L) = 2.2 \cdot 4.5K \cdot (17.5f + 50f)$$

$$= 660ps$$

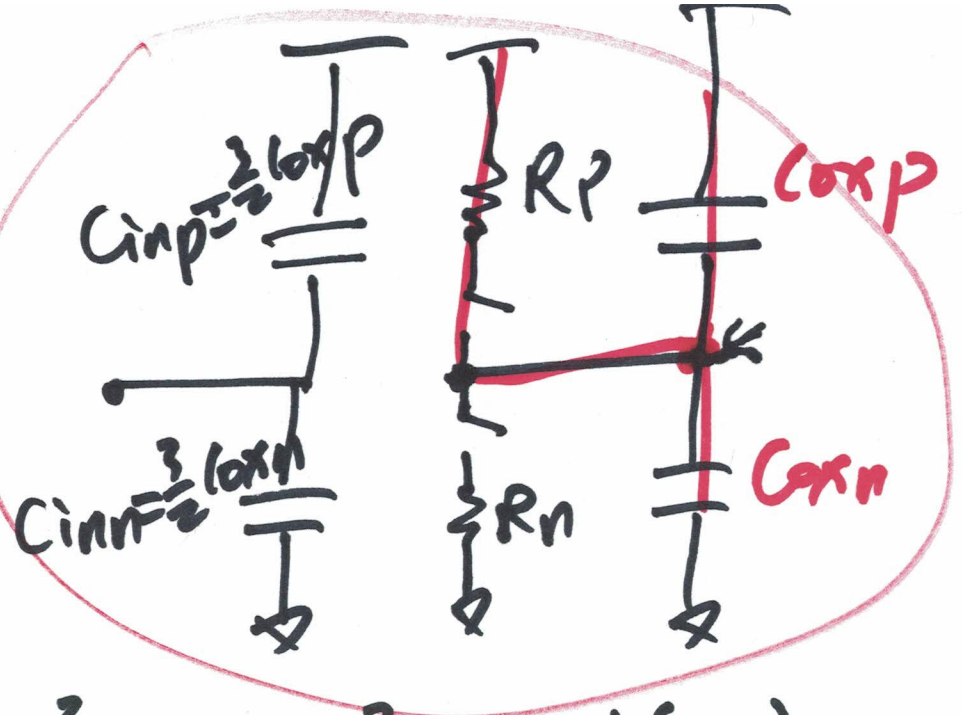
$R_p = 4.5K$
 $C_{exp} = 17.5fF$
 $C = \epsilon d$

$$t_{\text{prop}} = 0.7 \times 4.5K \times (17.5f + 50f)$$

$$= 210ps.$$

⑥

Miller Effect



$$C_{in} = C_{inn} + C_{inp} = \frac{3}{2} C_{oxn} + \frac{3}{2} C_{oxp} = \underline{\underline{\frac{3}{2} (C_{oxn} + C_{oxp})}}$$

$$\left. \begin{aligned} t_{pHL} &= 0.7 \cdot R_p \cdot (C_{oxn} + C_{oxp}) \\ t_{pHL} &= 0.7 R_n (C_{oxn} + C_{oxp}) \end{aligned} \right\}$$