

2's complement

$$\begin{array}{r}
 011 \\
 \downarrow\downarrow\downarrow \\
 100 \\
 + \\
 \textcircled{1}01 \\
 \hline
 \end{array}
 \quad
 \begin{array}{r}
 +3 \\
 \hline
 \end{array}
 \quad
 \textcircled{-3}$$

non-zero \rightarrow negative

$$\begin{array}{r}
 -4 + 2 + 0 = -2 \\
 \uparrow \\
 \textcircled{1}10 \quad -2 \\
 \hline
 101 \\
 \downarrow\downarrow\downarrow \\
 010 \\
 \hline
 \end{array}$$

$$\begin{array}{r}
 8 \\
 -2 \\
 \hline
 1 \quad \boxed{111111} = -1
 \end{array}$$

$$111 = -1$$

$$11 = -1$$

$$1 \dots 11 = -1$$

$$1010 = -6$$

$$\begin{array}{r}
 8 \\
 -2 \\
 \hline
 +2
 \end{array}$$

Ⓚ

$$\begin{array}{r}
 110 \quad -2 \\
 1111111110 = -2
 \end{array}$$

$$1111111110 = -2$$

$$00000001 = +1$$

overflow. (2's complement)

$$\boxed{\begin{array}{r} P \\ + P \\ \hline n \end{array} \quad \begin{array}{r} n \\ + n \\ \hline P \end{array}}$$

$$\begin{array}{r} P \\ + n \\ \hline P \end{array} \quad \times \quad \begin{array}{r} P & n \\ P & n \\ \hline P & n \\ \hline P & n \end{array}$$

$$\begin{array}{r} \textcircled{111} \\ + 100 \\ \hline 1011 \end{array}$$

$n-1$
 $n-4$ overflow occurs
 P
 -8 $+3$ -5 adopt C_2

$$\begin{array}{r} 111 \\ + 101 \\ \hline 1100 \end{array}$$

$n-1$ no overflow
 $n-3$
 $n-4$ duplicate S_2 to C_2
 S_2, S_0

$$\begin{array}{r} 011 \\ + 011 \\ \hline 0110 \end{array}$$

P 3
 P 3
 n

$$\begin{array}{r} 111 \\ + 011 \\ \hline 1010 \end{array}$$

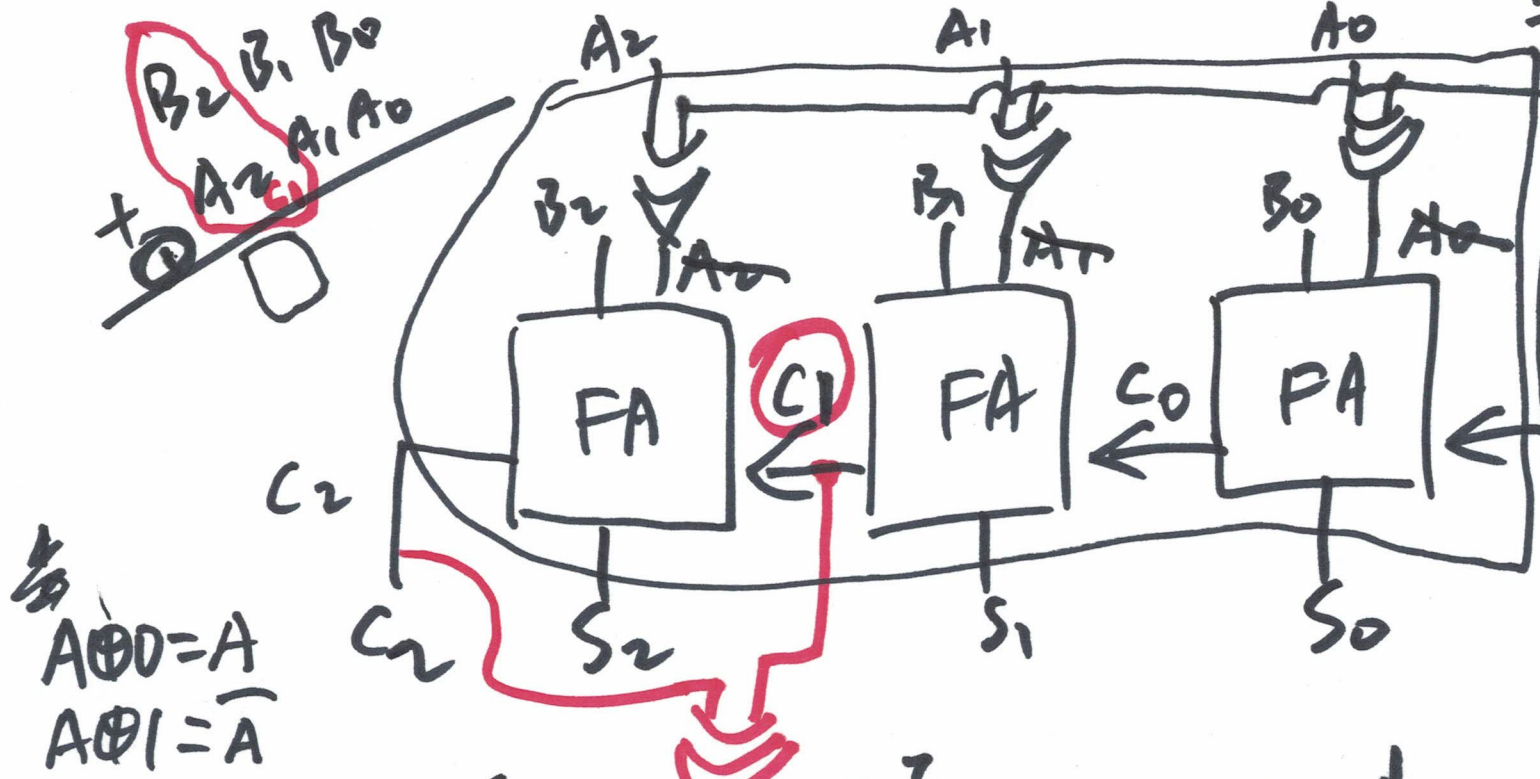
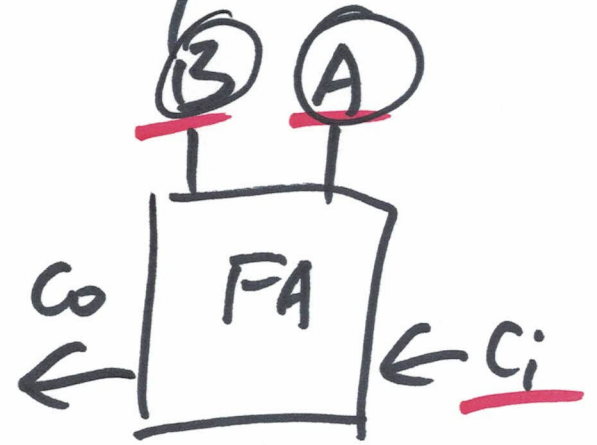
$n-1$
 P 3
 P 3
 P +2
 $-8+2=-6$
 10

$\{S_2, S_2, S_1, S_0\}$ ②

$\{C_2, S_2, S_1, S_0\}$

2's Complement 3-bit Adder/subtractor

FA: $C_0 = (A+B)C_i + AB$
 $S = A \oplus B \oplus C_i$



$A \oplus 0 = A$
 $A \oplus 1 = \bar{A}$

$A \oplus B = A + C - B$

{C2, S2, S1, S0} for unsigned

OV (3)

C_2	S_2	A_2	B_2	C_1	OV	Indicator (C_{2final})
0	0	0	0	0	0	0
0	1	0	0	1	1	0
0	1	0	1	0	0	1
1	0	0	1	1	0	0
0	1	1	0	0	0	1
1	0	1	0	1	0	0
1	0	1	1	0	1	1
1	1	1	1	1	0	1

overflow →

Method I: $OV = \bar{A}_2 \bar{B}_2 C_1 + A_2 B_2 \bar{C}_1$

Method II: $OV = C_1 \wedge C_2$

$C_{2final} =$
 $= \bar{C}_2 S_2 \bar{OV} + \bar{C}_2 S_2 OV$
 $+ C_2 \bar{S}_2 OV + C_2 S_2 \bar{OV}$

(4)

$$\begin{aligned}
 C_2 \text{ final} &= \overline{C_2} \underline{S_2 \overline{O} V} + C_2 \overline{S_2} \underline{O} V + C_2 \underline{S_2} \underline{O} V \\
 &= \cancel{(C_2 + C_2)} \cdot S_2 \overline{O} V + C_2 \overline{S_2} \underline{O} V \\
 &= S_2 \overline{O} V + C_2 \overline{S_2} \underline{O} V
 \end{aligned}$$

$\{C_2 \text{ final}, S_2, S_1, S_0\}$

